

ලොඞුලු සමාසය

අවකාශය A හි විවෘත නම් X හි A යන

- (D) X හි ලොඞුලු සමාසය හායිඩොල්ෆ් සමාසය
- (C) ඒකාකාරී ලොඞුලු සමාසය අවකාශය A අවකාශය ලෙසින්
- (B) ඒකාකාරී ලොඞුලු සමාසය හායිඩොල්ෆ් මෙට්‍රික් අවකාශය ලෙසින් සමාසය
- (A) ඒකාකාරී ලොඞුලු සමාසය

3. Which one of the following statements is

- (D) π ලොඞුලු
- (C) $\frac{\pi}{2}$ ලොඞුලු
- (B) $\frac{\pi}{4}$ ලොඞුලු
- (A) $\frac{\pi}{3}$ ලොඞුලු

4. If $a > 0$ then $\int_0^{\infty} \frac{x^a + a^x}{\log x} dx$ is equal to

- (D) $\frac{\pi}{2}$
- (C) ∞
- (B) $\frac{\pi}{4}$
- (A) 0

5. $\lim_{n \rightarrow \infty} \frac{1}{n} (1 + \sqrt[2]{2} + \sqrt[3]{3} + \dots + \sqrt[n]{n})$ is equal to

carries two (2) marks. All questions are compulsory.

Note : This paper contains seventy-five (75) objective type questions. Each question

$$e^{-\frac{\pi}{3u_5 x_5 t}} \cos\left(\frac{\pi}{u_5 x_5}\right)$$

$$(D) u(x, t) = \frac{\pi}{3} + \frac{\pi}{\sqrt{5}} \sum_{n=1}^{\infty} \frac{u}{n}$$

$$\sin\left(\frac{\pi}{u_5 x_5}\right)$$

$$(C) u(x, t) = \frac{\pi}{3} + \frac{\pi}{\sqrt{5}} \sum_{n=1}^{\infty} \frac{u}{n} e^{-\frac{\pi}{3u_5 x_5 t}}$$

$$e^{-\frac{\pi}{3u_5 x_5 t}} \cos\left(\frac{\pi}{u_5 x_5}\right)$$

$$(B) u(x, t) = \frac{\pi}{3} + \frac{\pi}{\sqrt{5}} \sum_{n=1}^{\infty} \frac{u}{(-1)^{n+1}}$$

$$e^{-\frac{\pi}{3u_5 x_5 t}} \cos\left(\frac{\pi}{u_5 x_5}\right)$$

$$(A) u(x, t) = \frac{\pi}{3} + \frac{\pi}{\sqrt{5}} \sum_{n=1}^{\infty} \frac{u}{(-1)^{n+1}}$$

$u^x(0, t) = u^x(\pi, t) = 0, u(x, 0) = 3x^2$ is
 $u^t = 3u^{xx}, 0 < x < \pi, t > 0,$

2. The solution to the heat equation

$$y = u_5, u = 1, 2, 3, \dots$$

(D) has non-trivial solutions if $y = 2u, u = 1, 2, 3, \dots$

(C) has no non-trivial solutions if $y = u, u = 1, 2, 3, \dots$

(B) has a non-trivial solution if

(A) has a non-trivial solution if $y \geq 0$

$$\frac{dx_5}{d_5 \lambda} + y\lambda = 0, \lambda(0) = 0, \lambda(\pi) = 0$$

4. The Sturm-Liouville problem



(C) \int_{-5}^5 (D) \int_{-5}^5

(A) \int_{-5}^5 (B) \int_{-5}^5

increment $\mu = 0.5$ is

given that $\frac{dx}{dt} = x + \lambda$, $\lambda(0) = 1$ with

Euler-Cauchy method of solution order

8. The value of $\lambda(0.5)$ obtained by

(D) $\phi(x) = f(x) + \frac{y_5 - 1}{y_5} \int_1^0 e_x \int_1^0 e_{-\lambda} f(\lambda) d\lambda$

(C) $\phi(x) = f(x) + \frac{y - 1}{y} \int_1^0 e_x \int_1^0 e_{-\lambda} \phi(\lambda) d\lambda$

(B) $\phi(x) = f(x) - \left(\frac{y - 1}{y + 1}\right) \int_1^0 e_x \int_1^0 e_{-\lambda} f(\lambda) d\lambda$

(A) $\phi(x) = f(x) - \frac{y - 1}{y} \int_1^0 e_x \int_1^0 e_{-\lambda} f(\lambda) d\lambda$

solution of (1) is

then which one of the following is the given real function $f(x)$ ($0 < x < 1$). If $y \neq 1$

$\phi(x) = f(x) + y \int_1^0 e_{x-\lambda} \phi(\lambda) d\lambda \dots (1)$ for a

9. Consider the Fredholm integral equation

(D) $\lambda(x) = e$

(C) $\lambda(x) = 0$

(B) $\lambda(x) = c$ where c is any real constant $\neq 0$

(A) $\lambda(x) = x$

$\int_p^q (x + \lambda_5 + 3\lambda_1) dx$ is given by

e. The extremal for the functional

(D) $(A \times B) \cup (C \times D) = (A \cup C) \times (B \cup D)$

(C) $(A \times B) \cap (C \times D) \subset (A \cup C) \times (B \cup D)$

(B) $(A \times B) \cup (C \times D) \supset (A \cup C) \times (B \cup D)$

(A) $(A \times B) \cap (C \times D) = (A \cup C) \times (B \cup D)$

then is

which one of the following statements is

10. If A, B, C, D are nonempty sets, then

(D) $\phi(t) \neq 0$ for all $t \in [a, b]$ with $t \neq t^0$ or $t^0 \neq t \in [a, b]$

(C) $\phi(t) \neq 0$ and $\phi'(t) = 0$ for all values

(B) $\phi(t) = 0 \quad \forall t \in [a, p]$
 $[a, p]$

(A) $\phi(t) \neq 0$ for atleast one value of t in

interval such that $\phi(t^0) = 0$. Then

$\phi = \begin{pmatrix} \phi^u \\ \cdot \\ \cdot \\ \cdot \\ \phi^s \\ \cdot \\ \phi^l \end{pmatrix}$ be a solution of the above

Let t_0 be any point of $[a, b]$ and let

$\frac{df}{dx^u} = s^{u1}(f)x^1 + \dots + s^{uu}(f)x^u$

$\cdot \quad \cdot \quad \cdot \quad \cdot$
 $\cdot \quad \cdot \quad \cdot \quad \cdot$
 $\cdot \quad \cdot \quad \cdot \quad \cdot$

$\frac{df}{dx^s} = s^{s1}(f)x^1 + \dots + s^{su}(f)x^u$

$\frac{df}{dx^l} = s^{l1}(f)x^1 + \dots + s^{lu}(f)x^u$

interval

a. Consider the homogeneous linear





- connected.
- (D) Every connected space is both connected and path connected.
- (C) The image of a connected space under a continuous map is connected.
- (B) The image of a connected space under a continuous map is connected.
- (A) The union of a collection of connected sets that have a point in common is connected.
- (B) The union of a collection of nonempty proper subsets A of X , where $A \cap B \neq \emptyset$, is connected.
- (A) If X is connected, then for every nonempty proper subset A of X , we have $A \cap B \neq \emptyset$.
14. Which one of the following statements is true?
- (D) The product of finitely many compact spaces is compact.
- (C) The image of a compact space under a continuous map is compact.
- (B) Every compact subspace of any topological space is closed.
- (A) Every compact subspace of any topological space is compact.
- (A) Every closed subspace of a compact space is compact.
13. Which one of the following statements is true?
- (D) Every subspace of a normal space is normal.
- (C) Product of two normal spaces need not be normal.
- (B) Every regular space is normal.
- (A) Every Hausdorff space is regular.
12. Which one of the following statements is true?
- (D) closed
- (C) path connected
- (B) bounded
- (A) compact
11. If A is a countable subset of \mathbb{R} with usual topology, then the set $\mathbb{R} - A$ is

- path connected.
- (D) No \mathbb{Q} -vector subspace of \mathbb{R} is a subspace of \mathbb{R} which are subfields is infinite.
- (C) Number of \mathbb{Q} -vector subspaces of \mathbb{R} are subfields of \mathbb{R} .
- (B) Only finitely many \mathbb{Q} -vector subspaces of \mathbb{R} are subfields of \mathbb{R} .
- (A) Every \mathbb{Q} -vector subspace of \mathbb{R} is a subfield of \mathbb{R} .
10. Let E be a finite Galois extension of the field of rational numbers \mathbb{Q} . Assume $[E : \mathbb{Q}] = 5$. Which one of the following statements is true?
- (C) $bd - b - d$ (D) $bd - 1$
- (A) $bd - b - d + 1$ (B) $bd - b - d - 1$
9. Let b and d be two distinct prime numbers. Then the number of integers a , $1 < a < bd$, which are coprime to bd is
- (D) Under the usual topologies, \mathbb{R} and \mathbb{C} are not homeomorphic to each other.
- (C) The mapping $f : [0, 1] \rightarrow \mathbb{S}^1$ defined by $f(t) = (\cos 2\pi t, \sin 2\pi t)$ is a homeomorphism.
- (B) $(-1, 1)$ and \mathbb{R} are homeomorphic.
- (A) The subspaces $[a, d]$ and $[0, 1]$ of \mathbb{R} are homeomorphic to each other.
8. Which one of the following statements is not true?



- 52 elements
- (D) irreducible over any finite field with elements
- (C) irreducible over the field \mathbb{F}_5 of five numbers \mathbb{F}
- (B) reducible over the field of real
- (A) irreducible over ring of integers \mathbb{Z}
50. The polynomial $f(x) = x_4 + x_3 + x_5 + x + 1$ is
- $a = p$
- (D) For $a, p, c \in B - \{0\}$, if $ac = pc$ then has a solution
- (C) The equation $x_5 = a, a \in B$ always group under multiplication
- (B) Non-zero elements can never be a always $a \in B$ such that $a \cdot c = p$
- (A) Given any $a, p \in B - \{0\}$ there is following holds :
51. In an integral domain B , which one of the zero ideal of \mathbb{Z} .
- $\mathbb{Z}[i]$, the intersection $\mathbb{Z} \cap \mathfrak{a}$ is a non-
- (D) For any non-zero prime ideal \mathfrak{a} of prime ideal.
- ideal generated by \mathfrak{a} in $\mathbb{Z}[i]$ is a
- (C) For any prime number \mathfrak{a} , in \mathbb{Z} , the extension of its prime field.
- $\mathbb{Z}[i] \setminus \mathfrak{a}$ is always a degree 2
- (B) If \mathfrak{a} is a prime ideal of $\mathbb{Z}[i]$, then $\mathbb{Z}[i] \setminus \mathfrak{a}$ is a field.
- (A) If \mathfrak{a} is a prime ideal of $\mathbb{Z}[i]$, then statements is true :
- integers. Which one of the following
52. Let $\mathbb{Z}[i]$ denote the ring of Gaussian

- (D) does not exist
- (C) exists, but not $\sqrt{3}$
- (B) is $\sqrt{3}$
- (A) is 3
- $A = \{p \in \mathbb{O} \mid p_5 < 3\}$ in \mathbb{O}

54. The supremum of the set
- relation
- (D) both transitive and symmetric
- (C) a symmetric relation
- (B) a transitive relation
- (A) an equivalence relation
- "a divides b" is
53. In the set of integers, the relation
- (D) \mathcal{C} cannot be a cyclic group
- (C) \mathcal{C} is a cyclic group
- (B) \mathcal{C} cannot be an abelian group
- (A) \mathcal{C} is an abelian group
- center. Assume $\mathcal{C} \setminus \Sigma$ is cyclic. Then
55. Let \mathcal{C} be a finite group and $\Sigma \subset \mathcal{C}$ be its
- (D) an associative ring
- identity
- (C) a non commutative ring without
- (B) a commutative ring with identity
- (A) a non-associative ring
57. The ring $M_5(\mathbb{R})$ of all 5×5 real matrices is



- (D) is $\sqrt[5]{5}$
 - (C) is 1
 - (B) is 0
 - (A) does not exist
37. $f(x) \rightarrow 0$ as $x \rightarrow \infty$. The $\lim_{x \rightarrow \infty} f'(x)$ $(0, +\infty)$, f is bounded on $(0, +\infty)$ and
38. Suppose f is twice differentiable on $(0, +\infty)$ and f is bounded on $(0, +\infty)$ and f'' is integrable function
- (D) f is a product of two Riemann-integrable functions
 - (C) $\int_a^b f(x) dx - \Gamma(b, f, \alpha) < \epsilon$ partition P such that
 - (B) for every $\epsilon > 0$, there exists a
 - (A) f is monotonic on $[a, b]$
39. Let α be monotonically increasing on $[a, b]$. Then the function $f: [a, b] \rightarrow \mathbb{R}$ is Riemann-integrable in regard to α if and only if
- (D) $\int_a^b \left(\log \left(\frac{x}{1} \right) \right) dx$
 - (C) $\int_a^b \frac{\sqrt[3]{1+5x}}{1-e^{-x}-1} dx$
 - (B) $\int_a^b e^{-x} dx$
 - (A) $\int_a^b \frac{\sqrt[4]{x}}{\log x} dx$
40. Which one of the following improper integrals diverges?
41. Which one of the following improper

- (D) is either 1 or -1
 - (C) is always 1
 - (B) may be any non-zero integer
 - (A) may not be an integer
- Then det(A)
- Assume that A^{-1} also has integer entries.
31. Let A be a 3×3 matrix with integer entries.
- (D) $\lim_{n \rightarrow \infty} x^n = 1$
 - (C) $\lim_{n \rightarrow \infty} n x^n = 5$
 - (B) $\lim_{n \rightarrow \infty} n x^n = 1$
 - (A) $\lim_{n \rightarrow \infty} n x^n = 0$
- monotonically. Then which the terms x^n decrease
32. Let $\sum_{n=1}^{\infty} x^n$ be a convergent series in
- (C) $\frac{5}{1}$
 - (D) 1
 - (A) 0
 - (B) $\frac{4}{1}$
33. The sum of the series $\sum_{n=1}^{\infty} \frac{u_4 + u_5 + 1}{n}$ is
- (D) Diverges for $a > \frac{3}{1}$
 - (C) Diverges for all real values of a
 - (B) Converges for $a > \frac{3}{1}$
 - (A) Converges for all real values of a
34. The series $\sum_{n=1}^{\infty} \left(\frac{u}{1} - \sin \left(\frac{u}{1} \right) \right)$



- T is diagonal with respect to which the matrix of
- (D) There may not be any basis of V diagonal with respect to which the matrix of T is diagonal
- (C) There is always a basis of V over the field of complex numbers with respect to which the matrix of T is diagonal
- (B) There is always a basis of V over the field of real numbers with respect to which the matrix of T is diagonal
- (A) The matrix of T is always diagonal
34. Let T be an endomorphism of a two dimensional vector space V over the field of rational numbers. Which one of the following is true ?
- (D) If A is invertible then the eigen values must be distinct
- (C) If A is invertible then the eigen values cannot be distinct
- (B) If A is invertible then there is always a non-zero real eigen value for A .
- (A) A is invertible if A has a non real, complex eigen value
35. Let A be a 2×2 real matrix. Then which of the following is true ?
- (D) $\text{End}^{\mathbb{F}}(V)$ always form a group under composition of endomorphisms
- (C) Non-zero endomorphisms of $\text{End}^{\mathbb{F}}(V)$ is always a \mathbb{F} -vector space under addition and composition of endomorphisms
- (B) $\text{End}^{\mathbb{F}}(V)$ can never be a commutative ring under usual structure
- (A) $\text{End}^{\mathbb{F}}(V)$ has no \mathbb{F} -vector space structure
36. Let T be an endomorphism of a two dimensional vector space V over the field of rational numbers. Which one of the following statements is true ?
- (D) $\text{End}^{\mathbb{F}}(V)$ denotes the set of all

$$(D) \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 0 \end{bmatrix}$$

$$(C) \begin{bmatrix} 0 & 0 & 0 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

$$(B) \begin{bmatrix} 0 & 5 & 0 \\ 1 & -1 & 0 \\ 1 & -1 & 0 \end{bmatrix}$$

$$(A) \begin{bmatrix} 0 & 5 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

with respect to the basis $\{1 + x, x, x^2\}$ is

$$T(t) = t^2 = \frac{qx}{qt}.$$

Then the matrix of T with respect to the basis $\{1 + x, x, x^2\}$ is

37. Let $E^5[x]$ be the vector space of all polynomials of degree at most 5 over a field F . Define $T : E^5[x] \rightarrow E^5[x]$ by

$$(D) \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix} \text{ and } \begin{bmatrix} 0 & 1 \\ 1 & 5 \end{bmatrix}$$

$$(C) \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix} \text{ and } \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$(B) \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} \text{ and } \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

$$(A) \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \text{ and } \begin{bmatrix} 0 & 0 \\ 3 & 0 \end{bmatrix}$$

over \mathbb{R} are similar ?

38. Which of the following pairs of matrices



(D) $\begin{pmatrix} \lambda & q \\ s & x \end{pmatrix}$ similar $\begin{pmatrix} \Sigma & c \\ p & m \end{pmatrix}$

(C) $\begin{pmatrix} \lambda & q \\ s & x \end{pmatrix}$ similar $\begin{pmatrix} x & q \\ s & \lambda \end{pmatrix}$

(B) $\begin{pmatrix} \lambda & s \\ q & x \end{pmatrix}$ similar $\begin{pmatrix} \Sigma & c \\ p & m \end{pmatrix}$

(A) $\begin{pmatrix} \lambda & p \\ s & x \end{pmatrix}$ similar $\begin{pmatrix} \Sigma & q \\ c & m \end{pmatrix}$

matrices can never be similar. λ and m , which form a basis of the following and m, x, λ and Σ represent any real

39. If $a < b < c < d$ are fixed real numbers

- (D) 4
- (C) 3
- (B) 5
- (A) 1

The dimension of V over \mathbb{R} is $a + b$

38. Let $\Lambda = \{(a, b, c, d) \mid a, b, c, d \in \mathbb{R}, a = c$

- (D) have absolute value 1
- (C) have multiplicity 5
- (B) are real
- (A) are purely imaginary

values of Λ

37. If $A = \begin{bmatrix} 1 & -3 & -4 \\ 0 & 5 & -3 \\ 1 & 0 & -1 \end{bmatrix}$ then the eigen

(D) Σe_4

(C) Σe_5

(B) $\Sigma(e_5 - e_4)$

(A) $\Sigma(e_4 - e_5)$

$|\Sigma| = 2$ positively oriented, is

$\int_C \frac{(z-1)(z-5)}{e^{5z}}$ where C is the circle

45. The value of the integral

(D) $\Sigma \cos(\alpha \sqrt{5})$

(C) $\sqrt{\Sigma} \cos(\alpha \sqrt{5})$

(B) $\Sigma \sin(\alpha \sqrt{5})$

(A) $\sqrt{\Sigma} \sin(\alpha \sqrt{5})$

then $|\Sigma|$ is

41. Suppose α is real and $\Sigma = 1 - \cos \alpha + i \sin \alpha$,

(D) $e_\Sigma + \Sigma$

(C) $\Sigma e_{1/\Sigma}$

(B) $e_\Sigma - i\Sigma$

(A) $e_\Sigma + i\Sigma$

$f(\Sigma)$ can be

for all $\Sigma \in \mathbb{C}$ and $u(x, \lambda) = \lambda + e_x \cos \lambda$. Then

40. Given that $f(\Sigma) = u(x, \lambda) + i v(x, \lambda)$ is analytic



- (D) Standard exponential
- (C) Degenerate at 1
- (B) Degenerate at 0
- (A) Uniform over [0, 1]

$\lambda = f(u)$, then what is the distribution of λ if U is uniform random variable over [0, 1], U and

49. If f is the probability density function of

- (D) an essential singularity at 1
- (C) a pole at 1 of order 5
- (B) a pole at 0 of order 5
- (A) a removable singularity at 1

$f(z) = (z-1)^5 \cdot e_{\frac{(z-1)^5}{z}}$. Then $f(z)$ has

42. Consider the complex valued function

- (D) $z = u\pi + (-1)^u \frac{\sqrt{5}}{u}, u \in \mathbb{Z}$
- (C) $z = u\pi + \frac{\sqrt{5}}{u}, u \in \mathbb{Z}$
- (B) $z = (-1)^u \cdot u\pi + \left(\frac{\sqrt{5}}{u} - \pi\right), u \in \mathbb{Z}$
- (A) $z = u\pi + (-1)^u \left(\frac{\sqrt{5}}{u} - \pi\right), u \in \mathbb{Z}$

$z \in \mathbb{C}$ are

44. The roots of the equation $\sin z = \cos 2z$,

- (D) 0
- (C) 4π
- (B) 1
- (A) 2π

$\int_C \frac{z-1}{f(z)} dz$ is

anticlockwise. Then the value of

43. Let $f(z) = z^3 - 1$ and C denote the circle of

- normal random variables
- (D) $X + \lambda$ and $X - \lambda$ are independent distribution
- (C) $(X + \lambda)(X - \lambda)$ has chi-square distribution
- (B) $X + \lambda$ and $X - \lambda$ are identically random variables
- (A) $X + \lambda$ and $X - \lambda$ are dependent

20. If X and Y are independent normal

- (D) $\frac{X+Y+\Sigma}{X}$ is Cauchy distribution
- (C) $X_\Sigma + Y_\Sigma + \Sigma_\Sigma$ has chi-square
- (B) $e_x + e_y + e_\Sigma$ is exponential
- (A) X given Y and Σ is normal

correct

distribution, which one of the following is

48. If (X, Y, Z) has tri-variate normal

- (D) Beta distribution
- (C) Uniform [0, 1] distribution
- (B) Degenerate distribution at 1
- (A) Degenerate distribution at 0

distribution over [0, 1] is converges to \cup having uniform

47. What does the distribution function of $\bigcup_{n=1}^{\infty} X_n$

- (D) Binomial $\left(\lambda, \frac{\Sigma}{\lambda}\right)$
- (C) Binomial $\left(\lambda, \frac{\pi}{\lambda}\right)$
- (B) Geometric $\left(\frac{\Sigma}{\lambda}\right)$
- (A) Poisson (Σ)

of X given $X + Y = 1$ is

random variables, what is the distribution

47. If X and Y are independent Poisson (Σ)



- moments finite
- (D) Student's t-distribution has all distribution generalization of Cauchy
- (C) Student's t-distribution is a
- (B) Student's t-distribution is symmetric sampling distribution
- (A) Student's t-distribution is a

23. Which of the following is not true ?

- (D) MGE of θ does not exist
- (C) Sample range is the MGE of θ
- (B) Sample mean is the MGE of θ
- (A) Sample median is the MGE of θ

the following is correct ?

$f(x;\theta) = \frac{1}{\sigma} e^{-|x-\theta|}$, $x \in \mathbb{R}$, $\theta \in \mathbb{R}$. Which of the probability density function

24. Let $\{X^1, \dots, X^n\}$ be a random sample from

- (D) $\frac{3}{2E+C}$
- (C) $\frac{4}{E+C}$
- (B) E/C
- (A) $\frac{5}{E+C}$

function ?

25. If E and C are distribution functions, which of the following is not a distribution

- (D) $\frac{2}{\sigma}$
- (C) $\frac{2}{\sigma}$
- (B) $\frac{2}{3}$
- (A) 1

what is $\lim_{n \rightarrow \infty} p_{(n)}^{11}$?

states 1, 2, given that $p^{12} = \frac{3}{5}$, $p^{21} = \frac{2}{5}$.

26. With reference to a Markov chain with

- (D) 1 is non-null
- (C) 1 is recurrent null
- (B) 1 is aperiodic
- (A) 1 is ergodic

sufficient condition for existence of a^1 ? in n-steps. Which of the following is a probability of going to state 1 from state 1

$a^1 = \lim_{n \rightarrow \infty} p_{(n)}^{11}$ where $p_{(n)}^{11}$ is the transition

27. Let 1 be a state of a Markov chain and

- (D) The errors have zero variances
- (C) The errors have zero expectations
- (B) The error variances are different
- (A) The error variances are same

heteroscedastic, mean ?

28. In a linear model, what does



- (D) $\frac{e}{\lambda}$
- (C) $\frac{3}{\lambda}$
- (B) $\frac{2}{\lambda}$
- (A) $\frac{2}{\lambda}$

is idle?

steady state probability that the system service rate λ and no waiting, what is the

28. In an M/M/1 queue with arrival rate λ ,

(D) $\left\{ B\left(\frac{\lambda}{t}\right), t \geq 0 \right\}$

(C) $\{ |B(t)|, t \geq 0 \}$

(B) $\{ e_{B(t)}, t \geq 0 \}$

(A) $\{ B(t+\lambda) - B(t), t \geq 0 \}$

is a Brownian motion?

Brownian motion, which of the following

28. If $\{B(t), t \geq 0\}$ denotes a standard

(D) $\sum_{n=1}^{\infty} b_{(n)}^{kk}$ converges to 0

(C) $\sum_{n=1}^{\infty} b_{(n)}^{kk}$ is divergent

(B) $\lim_{n \rightarrow \infty} b_{(n)}^{kk} = 0$

(A) $\sum_{n=1}^{\infty} b_{(n)}^{kk}$ converges

following?

Markov chain is which one of the

27. A criterion for state k to be recurrent in a

(D) $e_{f_s}, f \in \mathbb{R}$

(C) $e_{-f_s}, f \in \mathbb{R}$

(B) $e_{-|f|}, f \in \mathbb{R}$

(A) $e_{-f}, f \in \mathbb{R}$

$\frac{u}{X^1 + \dots + X^u}$ as $u \rightarrow \infty$?

of the characteristic function of

$\phi(f) = \begin{cases} 1 - |f| & \text{if } |f| \leq 1 \\ 0 & \text{if } |f| > 1 \end{cases}$ what is the limit

characteristic function

25. If X^1, X^2, \dots, X^u are independent with

(D) T^u is never unbiased for θ

regularity conditions

(C) T^u is consistent for θ under Cramer's

(B) T^u is never consistent for θ

(A) T^u is always unbiased for θ

is true?

distribution $F(\cdot; \theta)$, which of the following

21. If T^u is the MLE of a parameter θ in a

(D) $\lim_{f \rightarrow \infty} \frac{f}{N(f)} = \frac{h}{\lambda}$ a.s.

(C) $\lim_{f \rightarrow \infty} \frac{f}{N(f)} = h$ a.s.

(B) $\lim_{f \rightarrow \infty} \frac{f}{N(f)} = 0$ a.s.

(A) $\lim_{f \rightarrow \infty} \frac{f}{N(f)} = \lambda$ a.s.

h . Which of the following is true?

mean finite and mean inter-arrival time

20. Let $\{N(f), f \geq 0\}$ be a renewal process with



(D) $\frac{E(\lambda)}{-\text{COV}\left(\frac{X}{\lambda}, \lambda\right)}$

(C) $\frac{E(X)}{-\text{COV}\left(\frac{X}{\lambda}, \lambda\right)}$

(B) $\frac{E(\lambda)}{-\text{COV}\left(\frac{X}{\lambda}, X\right)}$

(A) $\frac{E(X)}{-\text{COV}\left(\frac{X}{\lambda}, X\right)}$

in a simple random sampling ;

82. What is the bias of the ratio estimator $\frac{X}{\lambda}$

(D) $\theta^4 = \theta^5 - \theta^3$

(C) $\theta^3 = \theta^4 + \theta^5$

(B) $\theta^5 = \theta^4 + \theta^3$

(A) $\theta^4 = \theta^5 + \theta^3$

$a\theta = a^4\theta^4 + a^5\theta^5 + a^3\theta^3$ estimable

when is the linear parametric function

$$A = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 5 \end{bmatrix}$$

84. Given the linear model $(Y, A\theta, \sigma^2 I^3)$ with

(C) 0.2

(D) -0.3

(A) -0.4

(B) 0.3

between $1 + X$ and $1 - 5Y$;

λ is 0.3, what is the correlation coefficient

83. If correlation coefficient between X and

(D) $\frac{94e_5}{51}$

(C) $\frac{94e_5}{81}$

(B) $\frac{94e_5}{11}$

(A) $\frac{35e_5}{51}$

If $(X + Y = 1)$ if X and Y are independent ; defined for appropriate values of t , what is

$M^X(t) = \left(\frac{t}{3 + e_t}\right)_3$ and $M^Y(t) = e_{5(e_t-1)}$

88. Given the moment generating functions

(D) 2

(C) 10

(B) 0

(A) -2

$x \geq 0, \lambda \geq 0$

minimize $x + \lambda$ subject to $x - \lambda = -2$, at an optimal solution of the LP.

87. Find the value of the objective function

contrast

(D) $a\alpha$ is an elementary treatment of the design matrix

(C) Vector a belongs to the row space space of the C-matrix of the design

(B) Vector a belongs to the column space of the design matrix

(A) Vector a belongs to the column effects alone, in a general block design ;

parametric function $a\alpha$ of treatment condition for estimability of a linear

86. What is a necessary and sufficient



free

(D) None of D^u , D_+^u , D_-^u are distribution free

(C) D_+^u and D_-^u are distribution free but

(B) D^u is distribution free but not D_+^u and D_-^u

(A) D^u , D_+^u and D_-^u are distribution free

following is true :

$D_-^u = \sup_x (F(x) - E^u(x))$, which of the

$D_+^u = \sup_x (E^u(x) - F(x))$,

$D^u = \sup_x |E^u(x) - F(x)|$,
distribution function. Let

F^u be the corresponding empirical
a continuous distribution function F and

10. Let $\{X^1, \dots, X^u\}$ be a random sample from

(D) 0

(C) $\frac{3}{4}$

(B) $\frac{5}{4}$

(A) 1

often) equal to :

$n = 1, 2, \dots$, what is $P\{X^u = 0\}$ infinitely

ea. Given that $P(X^u = 0) = \frac{5}{4} = 1 - P(X^u = 1)$,

(D) $P[|X| \geq \epsilon] \geq \frac{\epsilon_k}{E|X|_k}$

(C) $P[|X| \geq \epsilon] \leq \frac{\epsilon_k}{E|X|_k}$

(B) $P[|X| \leq \epsilon] \leq \frac{E|X|_k}{\epsilon_k}$

(A) $P[|X| \leq \epsilon] \geq \frac{\epsilon_k}{E|X|_k}$

13. Then the Markov inequality states that
Let X be a random variable with $E|X|_k < \infty$.

- (D) Median survival time of its components
- (C) Mean survival time of its components
- (B) Maximum of the survival times of its components
- (A) Minimum of the survival times of its components

15. In a parallel system of k components, the system survival time is

- (D) $\frac{\theta}{\sigma^u}$
- (C) $\sigma^u \cdot \theta$
- (B) $\sigma^u \cdot \theta^u$
- (A) $\frac{\theta^u}{\sigma^u}$

17. If T^u is a CAV estimator of θ with variance σ^u then $\log T^u$ is CAV for $\log \theta$ with



- (D) there is multicollinearity in the model
 are linearly independent
 (C) the columns of the regression matrix
 vector is singular
 (B) the dispersion matrix of the error
 (A) the errors are autocorrelated
- estimator is proposed when
 linear regression model, a ridge
 14. While estimating the parameters of a

- (D) $\sigma_b^2 = \frac{u-1}{b^2 d}$
 (C) $\sigma_b^2 = \frac{u-1}{u b d}$
 (B) $\sigma_b^2 = \frac{u}{b d}$
 (A) $\sigma_b^2 = \frac{u-1}{p d}$

variance of proportion p is
 proportion d of category II then the
 has proportion p of items of category I and
 dichotomous population. If the sample
 15. A sample of size n is drawn from a



ဥပဒေ နှင့် ဥပဒေရေးရာ
အဖွဲ့အစည်းများ



ඉපයේ සඳහා වූ
විදුලි ගාස්තුවක්

