Previous Year M.Sc., Degree Examinations September /October 2015

Directorate of Distance Education PHYSICS

DPA 510: Paper I: Mathematical Methods and Classical Mechanics

Time: 3 hrs] [Max.Marks: 75/85

Instructions:

- 1. Answer any FIVE questions from Parts A,B and C without omitting any Part.
- 2. Part D is compulsory for those who appear with maximum marks 85.

PART - A

Note: Answer any FIVE full questions.

- 1. a) Show that the function $f(z) = \sqrt{|xy|}$ is not regular at the origin although the Cauchy Riemann equations are satisfied at that point.
 - b) Prove Cauchy Integral theorem
 - c) Apply Calculus residues to prove that $\int_0^{2\pi} \frac{d\theta}{2 + \cos \theta} = \frac{2\pi}{\sqrt{3}}$ 5+5+5
- **2.** a) Prove the following orthogonal relation for Bessel's polynomials.

 $\int_0^a J_n (\mu r) J_n (\mu' r) r dr = 0 \text{ where } \mu \text{ and } \mu' \text{ are different roots of}$ $J_n (\mu \alpha) = 0$

b) Prove that
$$P_n(x) = (2n-1) \times P_{n-1}(x) - (n-1) P_{n-2}(x)$$
 8+7

- **3.** a) Discuss Gauss's divergence theorem.
 - b) Obtain Laplacian operator in spherical co-ordinate system. 8+7

PART - B

4. a) Define Hermitian matrix and unitary matrix. Show that every square matrix A can be uniquely expressed as the sum of a Hermitian and a Skew Hermitian matrix.

b) Find the inverse of the matrix
$$\begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$$
 8+7

- 5. a) Explain the law of transformation of second rank tensors.
 - b) State the quotient law for tensor. Illustrate the same with an example.
 - c) Obtain tensor form of Gradient.

5+5+5

6. a) Apply Fourier's series. for the expansion of $f(x) = x \sin x$ in the interval

$$-\pi \le x \le \pi$$
 hence deduce that $\frac{\pi}{4} = \frac{1}{2} + \frac{1}{1 \cdot 3} - \frac{1}{3 \cdot 5} + \frac{1}{5 \cdot 7}$

b) Show that Fourier transform of a Gaussian function is also Gaussian.

8+7

PART-C

- **7.** a) Starting with D'Alemberts principle, derive Lagrange's equations of motion for a conservative holonomic system.
 - b) What do you mean by the constrained motion of a system of particles?Classify the different kinds of constraints giving examples for each kind.8+7
- **8.** a) Define a central force. Show that angular momentum is a conserved quantity for a body in a central force field.
 - b) Discuss Rutherford scattering.

8+7

- **9.** a) Obtain the equation of motion of a particle in a central force field, obtain the orbit equation. Discuss the nature of orbits.
 - b) What are canonical transformations? Discuss canonical transformations in terms of the generating function F. **8+7**

PART-D

10. Answer any TWO of the following:

2 X 5=10

a) Using the generating function for Legendre polynomials, prove the recurrence relation:

$$P_{n+1}(x) - P_{n-1}(x) = (2n+1) P_n(x)$$

- b) Find the Eigen values and Eigen vectors of $A = \begin{pmatrix} \sin\theta & \cos\theta \\ -\cos\theta & \sin\theta \end{pmatrix}$
- c) Evaluate the Poisson braket $[L_x, P_y]$

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Previous M.Sc., Degree Examinations

September /October 2015

Directorate of Distance Education PHYSICS

DPA 520: Paper II: Quantum and Statistical Mechanics

Time: 3 hrs] [Max.Marks: 75/85

Instructions :

- 1. Answer any FIVE questions from Parts A,B and C without omitting any Part.
- 2. Part D is compulsory for those who appear with maximum marks 85.

PART - A

- **1.** a) Explain in brief, linear vector space, Hilbert space, linear operator and inner product of vectors.
 - b) Prove that i) Eigen values of a Hermitian operator are real ii) Eigen functions of a Hermitian operator corresponding to different eigen values are orthogonal

8+7

- 2. a) State and illustrate Ehrenfert's theorem.
 - b) What is the principle of superposition? Explain its significance.
- 3. a) Obtain the transmission coefficient (T) for a particle of energy $E < V_0$ in a finite height square potential barrier of width 2a for

$$V(x) = V_0 \text{ for } -a < x < a$$

= 0 for $|x| > a$

What happens to T when $V_0 \rightarrow \infty$?

b) Write a note on quantum mechanical tunneling.

12+3

PART - B

- **4.** a) Starting from the time independent Schrodinger equation for a one dimensional harmonic oscillator. Obtain the energy eigen values and eigen functions.
 - b) Show that the first order stark shift in a hydrogen atom is zero.

7+8

Contd...2

7+8

- **5.** a) Describe Stern-Gerlach experiment and explain its role in the development of quantum mechanics.
 - b) Evaluate the commutation relations i) $[L_x, L_y]$ and ii) $[L^2, L_z]$ 7+8
- **6.** a) Discuss the time dependent perturbation theory for a system of non-degenerate energy levels.
 - b) Using the appropriate expression for the first order coefficient $C_k^{(i)}(t)$, arrive at the Fermi golden rule. 7+8

PART - C

- **7.** a) Derive Maxwell-Boltzmann energy distribution formula for a gas of indistinguishable particles, in thermodynamic equilibrium at temperature T.
 - b) List out the criterion for distinguishability and indistinguishability. 11+4
- 8. a) What are macro and micro states of a statistical system? Explain.
 - b) State and prove Liouville theorem.
- 9. a) Explain Bose Einstein condensation and discuss its significance.
 - b) Arrive at Dulong and Petit's law using equipartition theorem. 8+7

PART - D

Answer any TWO of the following:

- **10.** a) Show that commuting observables with nondegenerate Eigenvalues have common set of Eigen functions.
 - b) What is Pauli exclusion principle? Explain.
 - c) Give the statistical interpretation of entropy. **2X5=10**

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Previous M.Sc., Degree Examinations

September /October 2015

Directorate of Distance Education PHYSICS

DPA530 Paper - III: Solid State Physics

Time: 3 hrs.] [Max.Marks:75/85

Instructions:

- 1. Answer any FIVE questions from Part A, B and C without omitting any Part.
- 2. Part D is compulsory for those who appear for paper with maximum marks 85.

PART - A

- **1.** a) What are point groups and space groups? Explain how one can deduce 32 point groups.
 - b) Obtain the Miller indices of a plane which intercepts at a, b/2, 3c in a simple cubic unit cell. Draw a neat diagram showing the plane (9+6)
- **2.** a) What is a structure factor? Calculate the structure factor for NaCl and Diamond.
 - b) Define the reciprocal lattice for the simple cubic lattice and show that the reciprocal of a reciprocal lattice is a direct lattice. (8+7)
- **3.** a) Discuss with examples the various crystal bindings exists in solids.
 - b) Give the Langevin theory of diamagnetism.

PART - B

- **4.** a) What are superconductors? Give an account on the specific heat in superconducting state.
 - b) Give the qualitative ideas of BCS theory of superconductivity. (8+7)
- **5.** a) Define polarization. Discuss the various microscopic polarization mechanisms in dielectrics
 - b) Derive the Lorentz Lorenz relation and comment on its importance (8+7)
- **6.** a) Discuss the failures of classical free electron theory of metals
 - b) Obtain an expression for thermal conductivity of metals and comment on the Wiedemann Franz law (7+8)

Contd...2

(7+8)

(5+5)

PART - C

- 7. a) Discuss the formation of energy bands in one dimensional periodic solids following Kronig Penny model.
 - b) Write a note on effective mass of electrons. (9+6)
- **8.** a) What are intrinsic semiconductors? Obtain an expression for the conductivity of an intrinsic semiconductor.
 - b) Obtain an equilibrium concentration for Frenkel defects. (8+7)
- **9.** a) Describe the Czochralski method of crystal growth.
 - b) Discuss the Neutron diffraction technique for the crystal structure analysis. (7+8)

PART - D

10. Write short notes on any TWO of the following:

- a) Primitive unit cell
- b) Ewald's sphere
- c) Hall effect

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Directorate of Distance Education PHYSICS

DPA540: Paper IV - Electronics

Time: 3 hrs.] [Max.Marks:75/85

Instructions:

- 1. Answer any FIVE questions from Part A, B and C without omitting any Part.
- 2. Part D is compulsory for those who appear for paper with maximum marks 85.

PART - A

- **1.** a) With the help of suitable circuit diagram, explain the mesh current and nodal method of network analysis.
 - b) Explain the terms: driving point impedance and transfer impedance of a multi mesh network.

 10+5
- 2. a) Define the characteristic impedance of an infinite ladder network. Obtain an expression for the characteristic impedance of π and T sections.
 - b) With a suitable example, explain active filter. What are the advantages of active filters over passive filters.

 8+7
- **3.** a) Obtain an expression for the characteristic impedance of a two wire transmission line. Explain the attenuation of radio frequency signals in a transmission line.
 - b) Obtain expressions for reflection coefficient and standing wave ratio of a transmission line. Calculate the reflection coefficient and standing wave ratio of infinite, short circuited and open circuited lines.

PART - B

- **4.** a) Explain the construction and working of a p-n junction diode. Explain the characteristics of a Zener diode. Discuss the design of a voltage regulator circuit using such a diode.
 - b) Discuss in detail the characteristics of a FET.

9+6

- **5.** a) With neat circuit diagrams explain briefly the design and working principles involved in the construction of a C-E and C-C amplifier.
 - b) Discuss the different biasing methods employed in transistor amplifiers. 9+6
- 6. a) Discuss the feedback requirements and criteria for oscillation in transistor oscillator. With a neat circuit diagram explain the working of a Wien Bridge oscillator,
 - b) Explain the principle of working of a stable, monostable and bistable multivibrators.

 9+6

PART - C

- 7. a) Discuss the characteristics of an ideal operational amplifier. With suitable circuit diagrams explain the working of an inverting and non inverting amplifiers.
 - b) Explain the working principles of opamp based Wein bridge and phase shift oscillators.

 9+6
- **8.** a) With reference to digital electronics, explain with examples the following terms: i) number systems and codes, ii) hexadecimal and octal, iii) BCD, grey codes and excess-3 codes,
 - b) Explain the working of I) adder and subtractor circuits, ii) differentiator and integrator.10+5
- **9.** a) Explain how Karnaugh maps are employed in the simplification of a logic function. Give an example
 - b) Discuss the action of AND, OR, NOR, NOT, NAND and XOR logic gates with suitable truth tables.

 6+9

PART - D

10. Answer any TWO of the following:

- a) Regulated power supply.
- b) Flip-flop circuits
- c) Thevenin's and Norton's theorem.

 $2 \times 5 = 10$