



PD – 090

**II Year M.Sc. (DCC) Degree Examination, January 2018
(Fresh and Repeaters) (Y2K13 Scheme)
MATHEMATICS
M202 : Numerical Analysis**

Time : 3 Hours

Max. Marks : 80

- Instructions:** 1) Answer **any five** questions, choosing at least **two** from **each** Part.
2) **All** questions carry **equal** marks.

PART – A

1. a) Find the smallest root of the equation $f(x) = 3x - \cos x - 1 = 0$ correct to four decimals.
- b) Determine a quadratic factor of the polynomial $x^4 + x^3 + 2x^2 + x + 1 = 0$ with $p_0 = 0.5 = q_0$. **(8+8)**
2. a) Explain the procedure of Gauss-elimination method for solving the system of equations and hence solve
- $$2x_1 + 2x_2 + x_3 + 2x_4 = 7$$
- $$x_1 - 2x_2 - x_4 = 2$$
- $$3x_1 - x_2 - 2x_3 - x_4 = 3$$
- $$x_1 - 2x_4 = 0.$$
- b) Find the roots of
- $$x^2 - y^2 = 4$$
- $$x^2 + y^2 = 16$$
- with $x_0 = y_0 = 2\sqrt{2}$. **(8+8)**

P.T.O.



3. a) With help of the following table :

x	: -1	0	1
f(x)	: 1	1	3
f'(x)	: -5	1	7

Find $f(-0.5)$ and $f(0.5)$ using the Hermite interpolation.

- b) Obtain the Rational approximation $R_{5,4}$ for e^{-x} . **(8+8)**

4. a) Derive the Gauss-Legendre three point integration formula and hence

evaluate $\int_{-1}^1 (1-x^2)^{3/2} \cos x \, dx$.

- b) Evaluate : $\int_0^1 \int_0^x 4xy \, dy \, dx$ using Simpson's $\frac{1}{3}$ rule with three subintervals. **(8+8)**

PART – B

5. a) Derive the Runge-Kutta fourth order method and hence solve $\frac{dy}{dx} = \frac{x^2}{y^2 + 1}$,
 $y(0) = 0$ at $x = 0.2$. Take $h = 0.1$.

- b) Using the Runge-Kutta second order method, solve

$$\frac{dy}{dx} = -3y + 2z, \quad y(0) = 0$$

$$\frac{dz}{dx} = 3y - 4z, \quad z(0) = 0.5$$

with $h = 0.2$. Obtain the solution at $x = 0.4$.

(8+8)

6. a) Solve the boundary value problem $y'' = xy$, $y(0) = y'(0) = 1$, $y(1) = 1$ with

$$\Delta x = \frac{1}{3} \text{ using finite difference method.}$$



b) Solve the one-dimensional equation $U_t = U_{xx}$, $0 \leq x \leq 1$, $t \geq 0$ with

$$U(x, 0) = \sin 2\pi x; 0 \leq x \leq 1$$

$$U(0, t) = 0 = U(1, t), t \geq 0$$

using Crank-Nicolson method.

Take $\Delta x = \frac{1}{4}$, $\Delta t = \frac{1}{36}$. Obtain the solution at second time level. **(8+8)**

7. Derive the alternating direction implicit scheme applied to the two dimensional parabolic equation. Also discuss its stability issues. **16**

8. a) Discuss the stability of the finite difference scheme applied to the one-dimensional wave equation.

b) Solve the Poisson's equation $U_{xx} + U_{yy} = \sin \pi x \sin \pi y$, $0 \leq x, y \leq 1$ subjected

to the conditions $U = 0$ on the boundary. Take $\Delta x = \Delta y = \frac{1}{3}$. **(6+10)**
